

# Ultra High Density Wireless Cells

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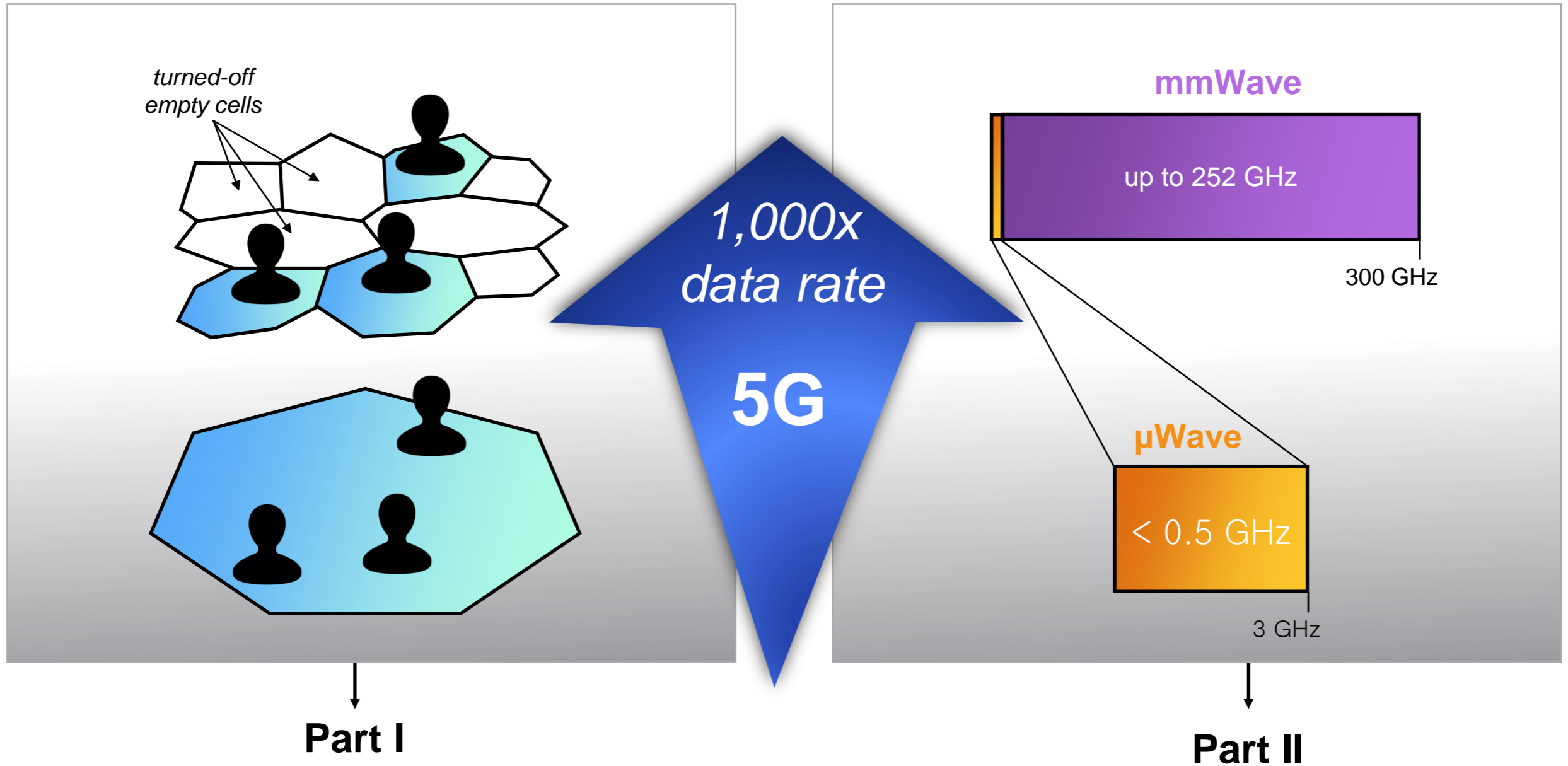
## 5G Cellular Network Enablers:

### 1. Base Station (BS) Ultra-Densification

[Qualcomm13, 14]

### 2. Millimeter-Wave (mmWave) Overlay

[Rappaport13], [Samsung11]



[Qualcomm14] Qualcomm, "Hyper-Dense Small Cell Deployment Trial in NASCAR Environment," April 2014.

[Qualcomm13] I. Hwang, B. Song, and S. S. Soliman, "A Holistic View on Hyper-Dense Heterogeneous and Small Cell Networks," IEEE Comm. Mag., 2013.

[Rappaport13] T. S. Rappaport, et. al., "Millimeter Wave Mobile Communications for 5G Cellular: It Will Work!," IEEE Access, 2013.

[Samsung11] Z. Pi and F. Khan, "An Introduction to Millimeter-Wave Mobile Broadband Systems," IEEE Comm. Mag., 2011.

Part I.

# Asymptotic Behavior of Ultra-Dense Cellular Networks and Its Economic Impact [GC14]

- Spectral Efficiency (SE) in downlink ultra-dense cellular networks
- Profit maximizing BS & spectrum OPEX

[GC14] J. Park, S.-L. Kim, and J. Zander, "Asymptotic Behavior of Ultra-Dense Cellular Networks and Its Economic Impact," *to appear in Proc. IEEE GLOBECOM 2014*.

# Motivation

## Downlink Cellular Network Average Spectral Efficiency (SE)

$$\text{Average Rate} = \text{Spectrum Amount} \times \text{SE}$$

1. Sparse network ( $\lambda_u \gg \lambda_b$ ): **independent of BS density** [Andrews11]
2. Dense network: **increasing function** of BS density with diminishing returns [SMYu13], [SLee12]
3. Ultra-Dense network ( $\lambda_u \ll \lambda_b$ ): **?**

[Andrews11] J. G. Andrews, F. Baccelli, and R. K. Ganti, "A Tractable Approach to Coverage and Rate in Cellular Networks," IEEE Trans. on Comm., 2011.

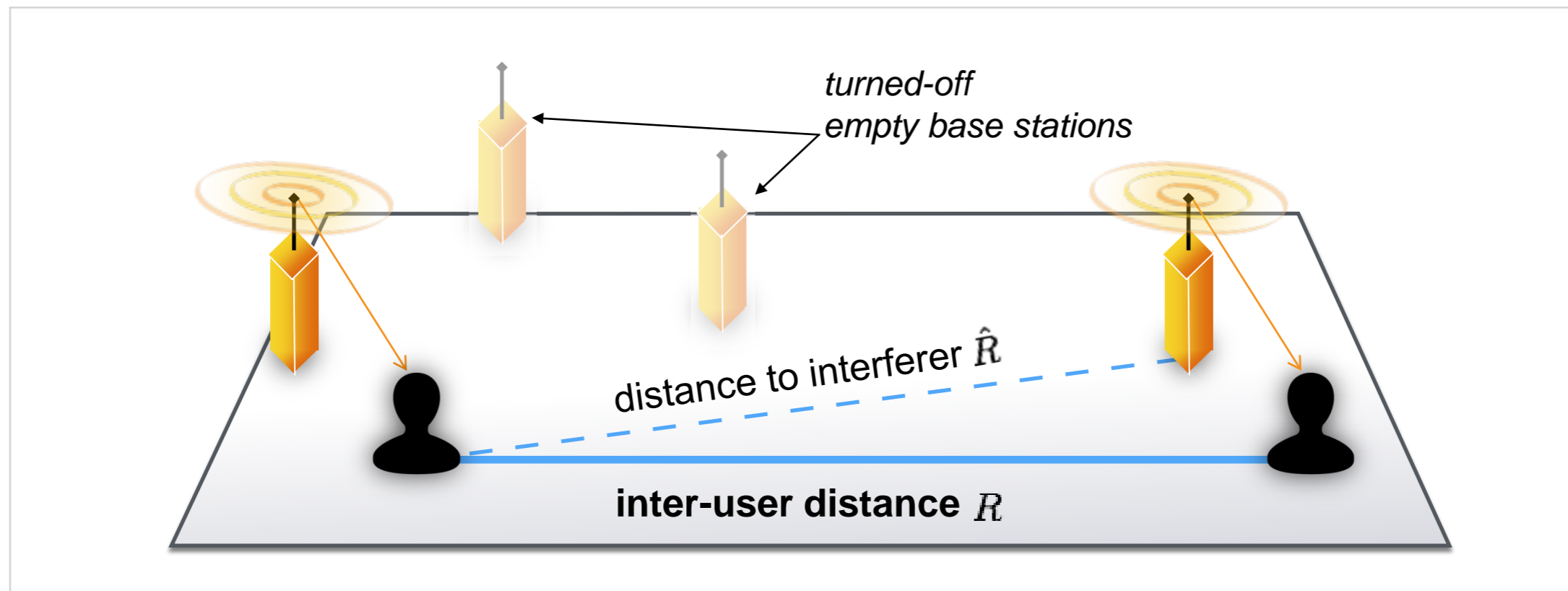
[SMYu13] S. M. Yu and S.-L. Kim, "Downlink Capacity and Base Station Density in Cellular Networks," Proc. IEEE WiOpt Workshop on SpaSWIN 2013, May 2013.

[SLee12] S. Lee and K. Huang, "Coverage and Economy of Cellular Networks with Many Base Stations," IEEE Comm. Letters, 2012.

# Motivation

## User Location Dependent Interferers in Ultra-Dense Networks

Interferer locations converge to the user locations ( $\hat{R} \rightarrow R$ ), under dormant mode operation [Ericsson13]



# System Model

- BS locations ~ homogeneous Poisson point process (PPP) with density  $\lambda_b$
- User locations ~ homogeneous PPP with density  $\lambda_u$
  
- Maximum SNR (nearest) association
- Dormant operation when BSs being empty
- Uniformly random scheduler
  
- Path loss attenuation, Rayleigh fading
- Interference-limited regime (consider SIR instead SINR)

# SE in Sparse and Ultra-Dense Networks

## BS Density Increase Effect on SE

### Sparse network SE

(w.o. multiple access)

$$\gamma_\alpha = \int_0^\infty [1 + \rho_t (e^t - 1)^{\frac{\alpha}{2}}]^{-1} dt$$

**independent of BS density**

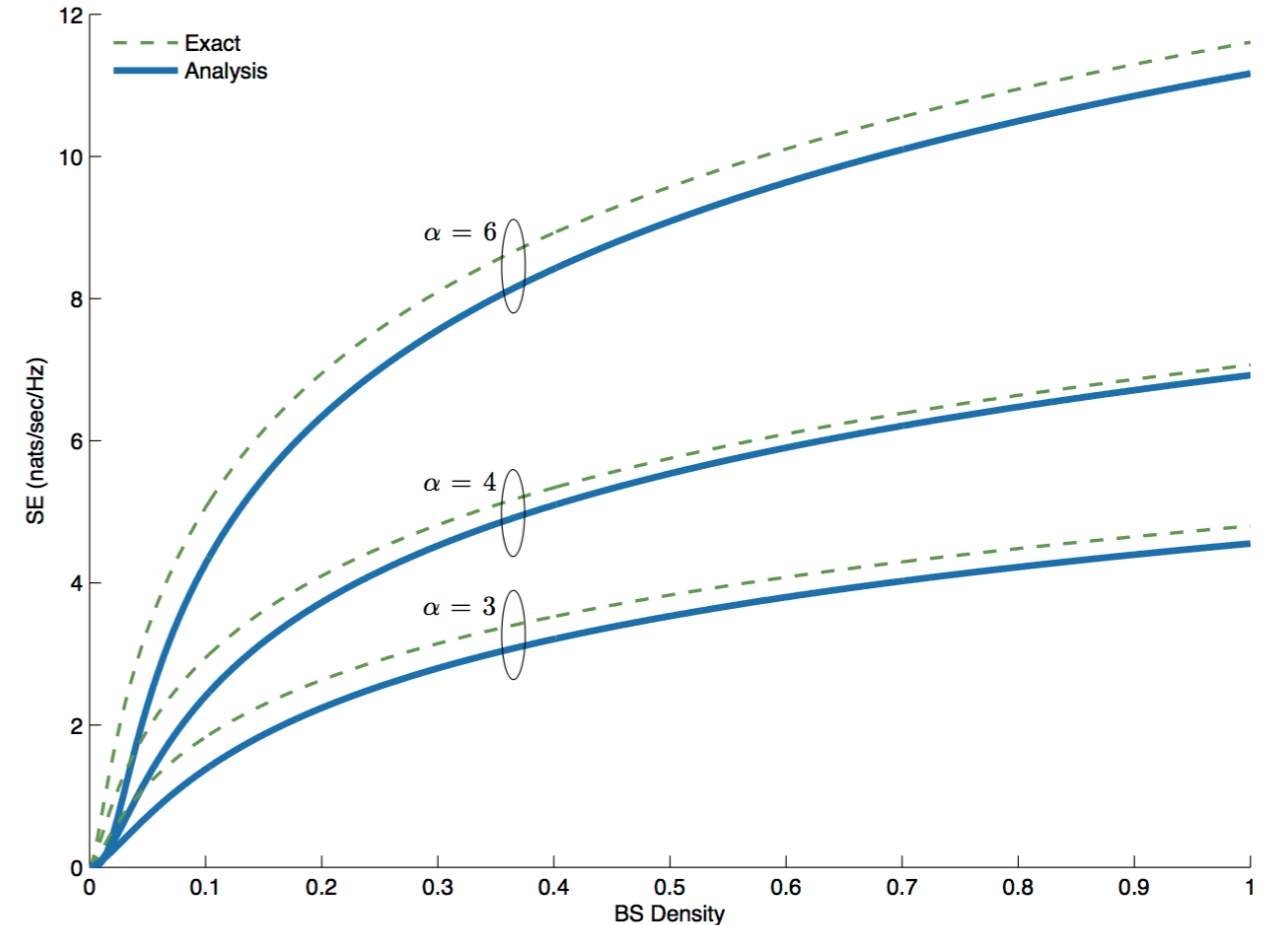
(w. multiple access)

$$\gamma \approx \frac{\lambda_b}{\lambda_u} \gamma_\alpha$$

### Ultra-dense network SE

$$\gamma \gtrsim \log \left[ 1 + \left( \frac{\lambda_b}{\rho_0 \lambda_u} \right)^{\frac{\alpha}{2}} \right]$$

$$\text{where } \rho_0 := \int_0^\infty 1 / (1 + u^{\frac{\alpha}{2}}) du$$



# SE in Sparse and Ultra-Dense Networks (w. Multiple Access)

## User Density Increase Effect on SE

*Sparse network SE*

(w.o. multiple access)

$$\gamma_\alpha = \int_0^\infty [1 + \rho_t (e^t - 1)^{\frac{\alpha}{2}}]^{-1} dt$$

(w. multiple access)

$$\gamma \approx \frac{\lambda_b}{\lambda_u} \gamma_\alpha$$

**∴ multiple access congestion**

*Ultra-dense network SE*

$$\gamma \gtrsim \log \left[ 1 + \left( \frac{\lambda_b}{\rho_0 \lambda_u} \right)^{\frac{2}{\alpha}} \right]$$

**∴ interference increment**



# Profit Maximizing BS & Spectrum OPEX

## User Demand Model

- Usage-based pricing: price  $p$  per bit
- Willingness-to-pay:  $\Theta \sim \text{uniform}(0, b)$

where **rate sensitivity**  $b > p$

- Rate (demand) per user:  $X$

- Payoff function:

$$U = [\theta \log(1 + X) - pX]^+$$

## 3-Stage Profit Maximization

$$\begin{aligned} \text{(P1) : Maximize} & \quad \text{revenue} & \quad \text{OPEX} \\ & \quad p\lambda_u \bar{X} & - (c_b \lambda_b + c_w W) \\ \text{subject to} & \quad \bar{X} \leq W\gamma \\ & \quad \text{avg. demand} & \quad \text{avg. rate (supply)} \end{aligned}$$

comprising 3 stages

### Stage 3.

*rate decision* — operator's profit maximizing  
base station density and spectrum amount

### Stage 2.

*price decision* — operator's profit maximizing price

### Stage 1.

*demand prediction* — user's payoff maximizing rate

*network operation*

*profit maximization*

# Optimal Price (Stages 1 & 2)

## Demand Prediction

- avg. user demand per user) at Stage 1

$$\bar{X} = \frac{(b - p)^2}{2bp}$$

- per-user demand *decreases with*  $p$  ( $\because b > p$ )

- its resultant profit in (P1) also *decreases with*  $p$

$$\begin{aligned} \text{(P1) : Maximize} & \quad \overset{\text{revenue}}{p\lambda_u\bar{X}} - \overset{\text{OPEX}}{(c_b\lambda_b + c_wW)} \\ & \text{subject to} \quad \bar{X} \leq W\gamma \\ & \quad \text{avg. demand} \quad \text{avg. rate (supply)} \end{aligned}$$

*optimal price occurs when  
the (P1) constraint's equality holds*

## Optimal Price at Stage 2

$$p^* \approx \frac{b}{2(1 + W\gamma)}$$

# Profit Optimal BS Density & Spectrum Amount (Stage 3)

## OPEX Effect

Result 1. (Unit Cost) Optimal BS density and spectrum amount are:

- inversely proportional to their unit costs
- proportional to their counter resource unit costs

$$\begin{aligned} \text{Sparse: } & \begin{cases} \lambda_b^* = \left[ \frac{bc_w}{2\gamma\alpha} \left( \frac{\lambda_u}{c_b} \right)^2 \right]^{\frac{1}{3}} \\ W^* = \left[ \frac{bc_b}{2\gamma\alpha} \left( \frac{\lambda_u}{c_w} \right)^2 \right]^{\frac{1}{3}} \end{cases} \\ \text{Ultra-Dense: } & \begin{cases} \lambda_b^* \approx \left[ \left( \frac{\alpha}{2^{2.5}c_b} \right)^8 (bc_w)^4 \rho_0^\alpha \lambda_u^{\alpha+4} \right]^{\frac{1}{\alpha+8}} \\ W^* \approx \left[ 2^{2(\alpha-2)} \frac{c_b^\alpha}{c_u^{\alpha+4}} b^4 \rho_0^\alpha \lambda_u^{\alpha+4} \right]^{\frac{1}{\alpha+8}} \end{cases} \end{aligned}$$

# Profit Optimal BS Density & Spectrum Amount (Stage 3)

## OPEX Effect

Result 2. (OPEX Ratio) Operators should invest in BS OPEX:

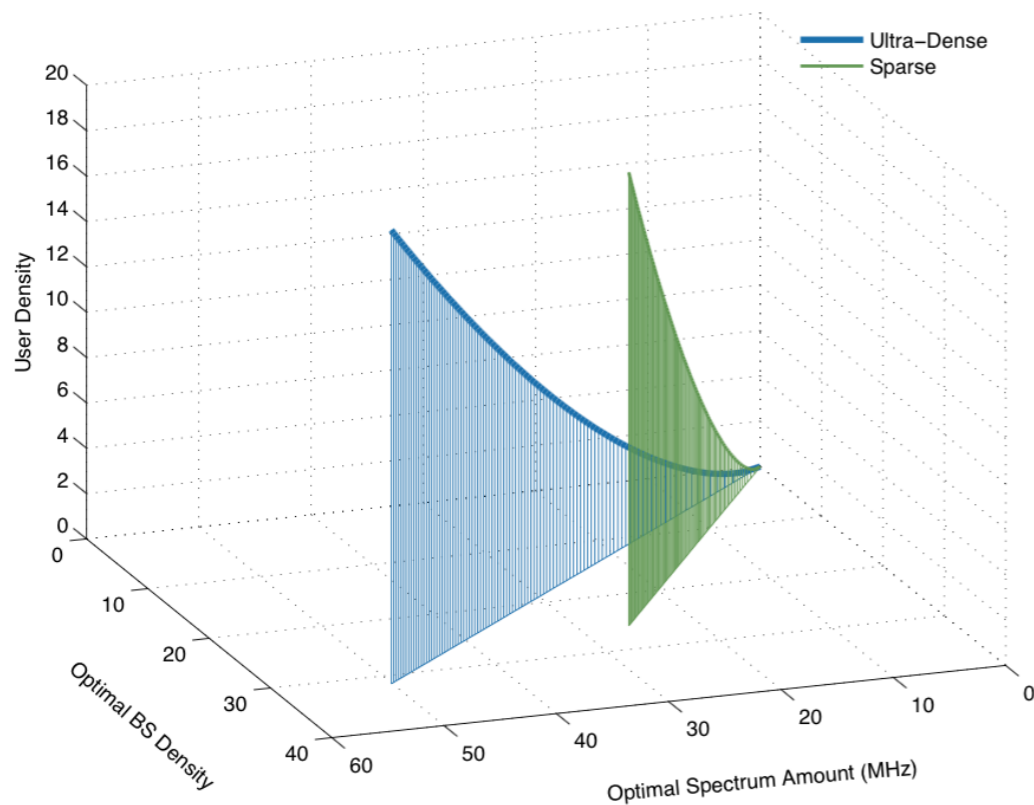
1) as much as spectrum OPEX for sparse networks

$$\text{Sparse: } \frac{c_b \lambda_b^*}{c_w W^*} = 1$$

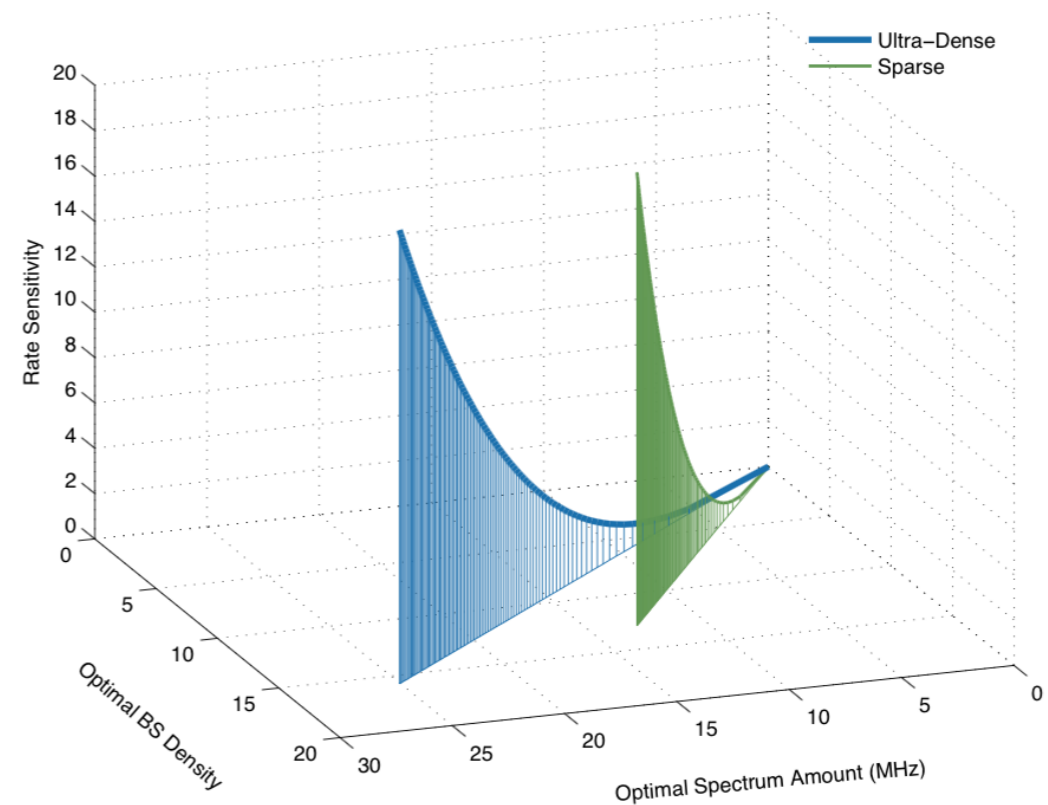
0.43 ~ 0.71

2) less than spectrum OPEX for ultra-dense networks

$$\text{Ultra-Dense: } \frac{c_b \lambda_b^*}{c_w W^*} \approx 2^{-2} \alpha^{\frac{8}{\alpha+8}}$$



(a) For user density  $\lambda_u$  for  $b = 10$



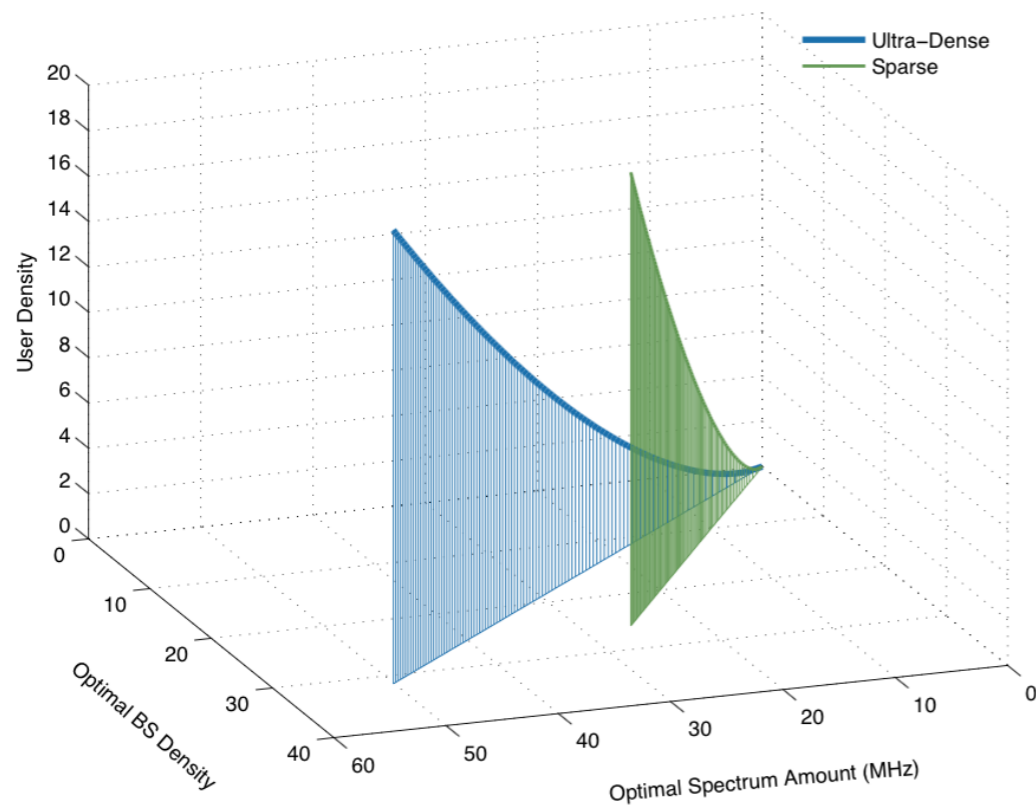
(b) For per-user rate sensitivity  $b$  for  $\lambda_u = 5$

Fig. 3. Profit optimal BS density  $\lambda_b^*$  and spectrum amount  $W^*$  ( $\alpha = 4$ ,  $c_b = c_w = 0.1$ ).

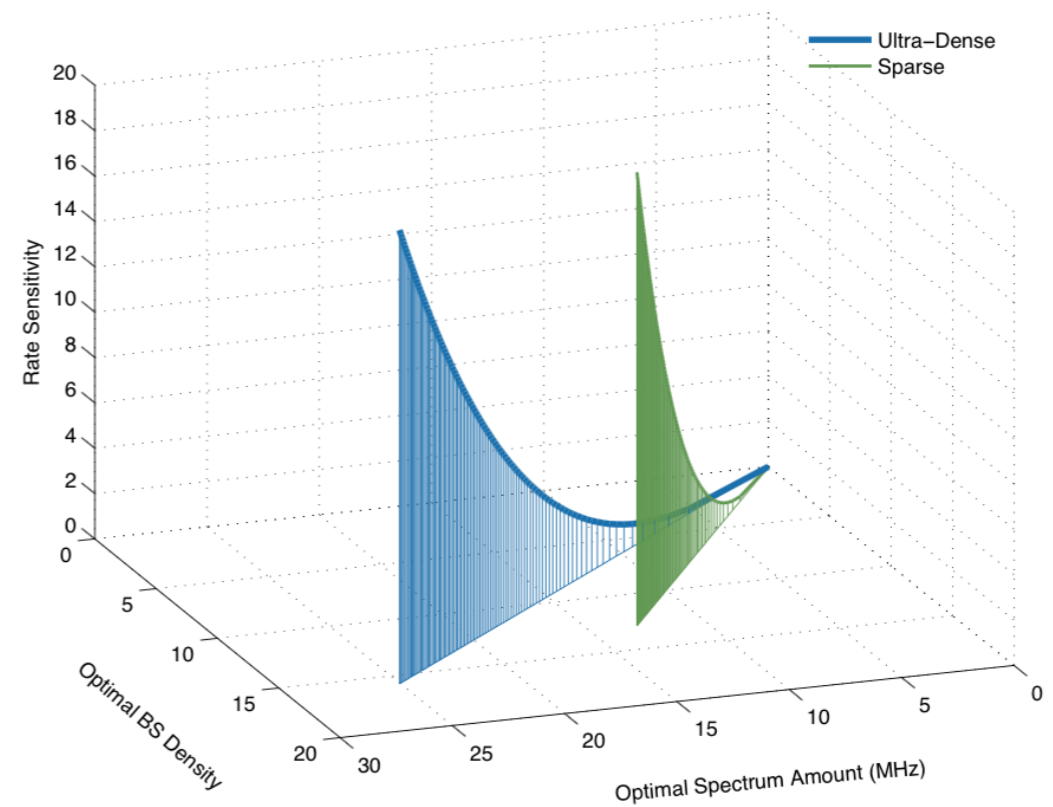
# Profit Optimal BS Density & Spectrum Amount (Stage 3)

## User Demand Effect: User Density vs. Rate Sensitivity

Result 3. (Increasing Rate) Both profit optimal BS density and spectrum amount increase with user density higher than rate sensitivity



(a) For user density  $\lambda_u$  for  $b = 10$



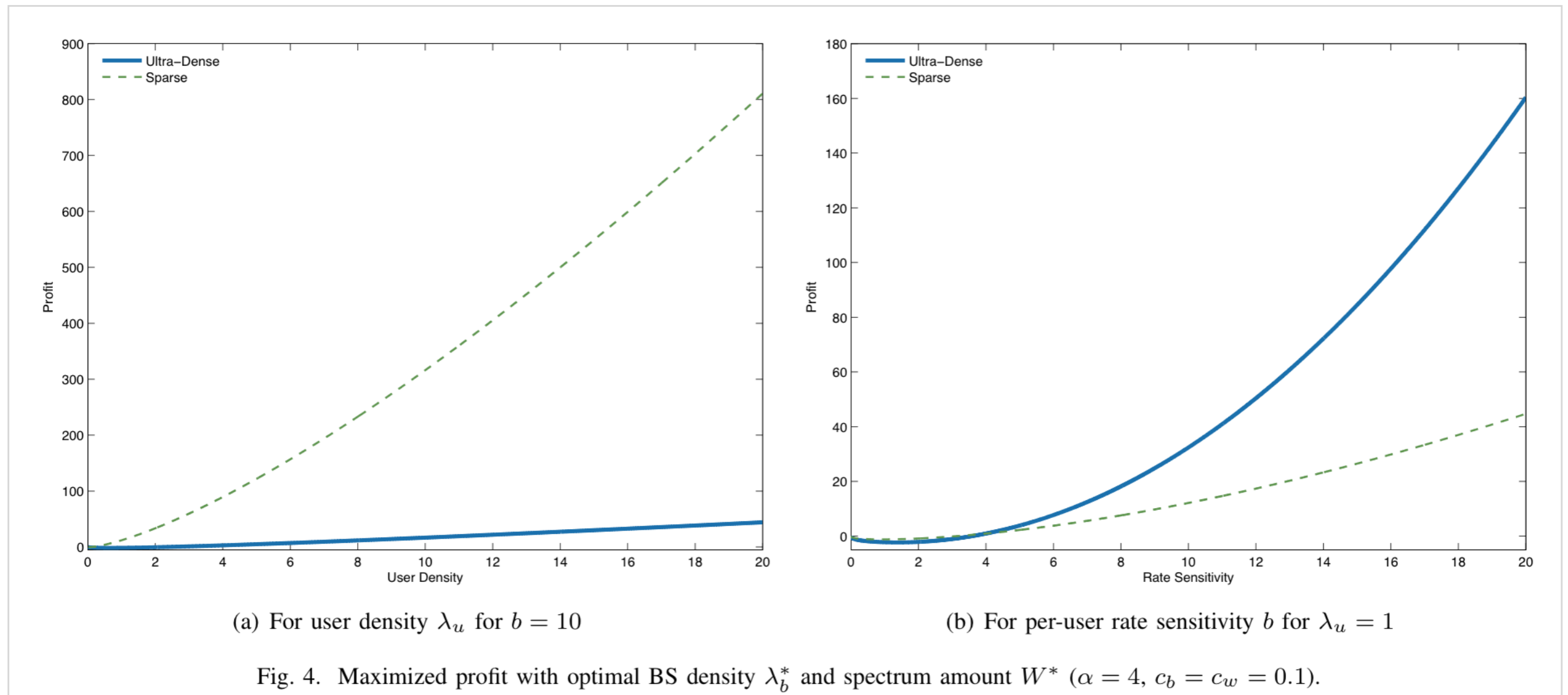
(b) For per-user rate sensitivity  $b$  for  $\lambda_u = 5$

Fig. 3. Profit optimal BS density  $\lambda_b^*$  and spectrum amount  $W^*$  ( $\alpha = 4$ ,  $c_b = c_w = 0.1$ ).

# Profit Optimal BS Density & Spectrum Amount (Stage 3)

## User Demand Effect: User Density vs. Rate Sensitivity

Result 4. (Ultra-Dense Network Profitability) Ultra-densification is not preferable for user density increase but for rate sensitivity increase



Part II.

# Resource Management and Cell Planning in Millimeter-Wave Overlaid Ultra-Dense Cellular Networks [JSAC14]

- mmWave overlaid ultra-dense cellular network design
- Uplink/downlink SE
- Uplink/downlink resource allocations
- Required BS density scaling law

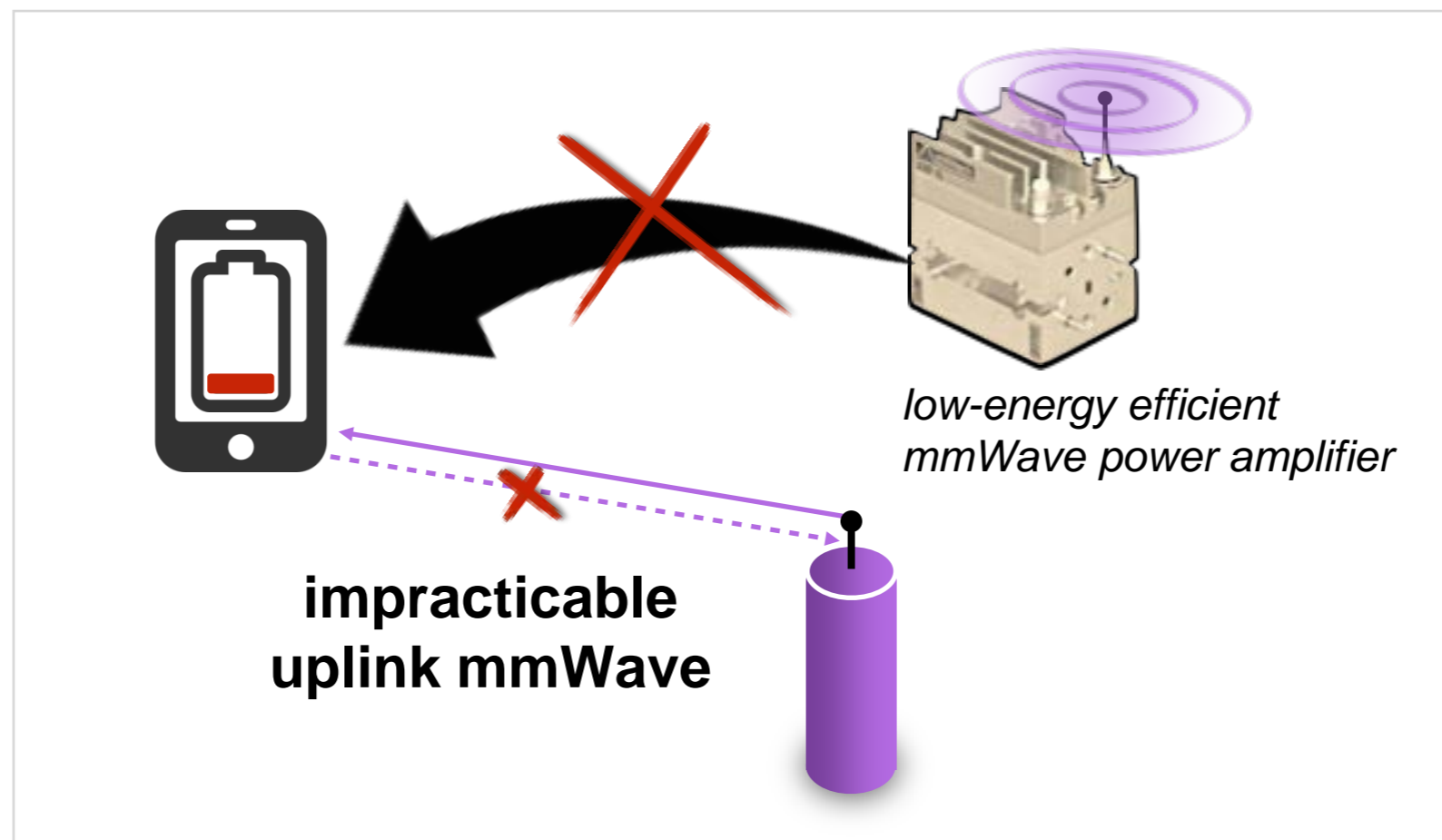
[JSAC14] J. Park, S.-L. Kim, and J. Zander, "Resource Management and Cell Planning in Millimeter-Wave Overlaid Ultra-Dense Cellular Networks," submitted to IEEE JSAC.

# Motivation

- No micro-wave ( $\mu$ Wave) & mmWave coexisting network analysis
- No closed-form uplink/downlink SE

\* **Uplink/downlink rate asymmetry** [Samsung11, 13]

mmWave resorts to be implemented for downlink transmission only



[Samsung11] Z. Pi and F. Khan, "An Introduction to Milimeter-Wave Mobile Broadband Systems," IEEE Comm. Mag., June 2011.

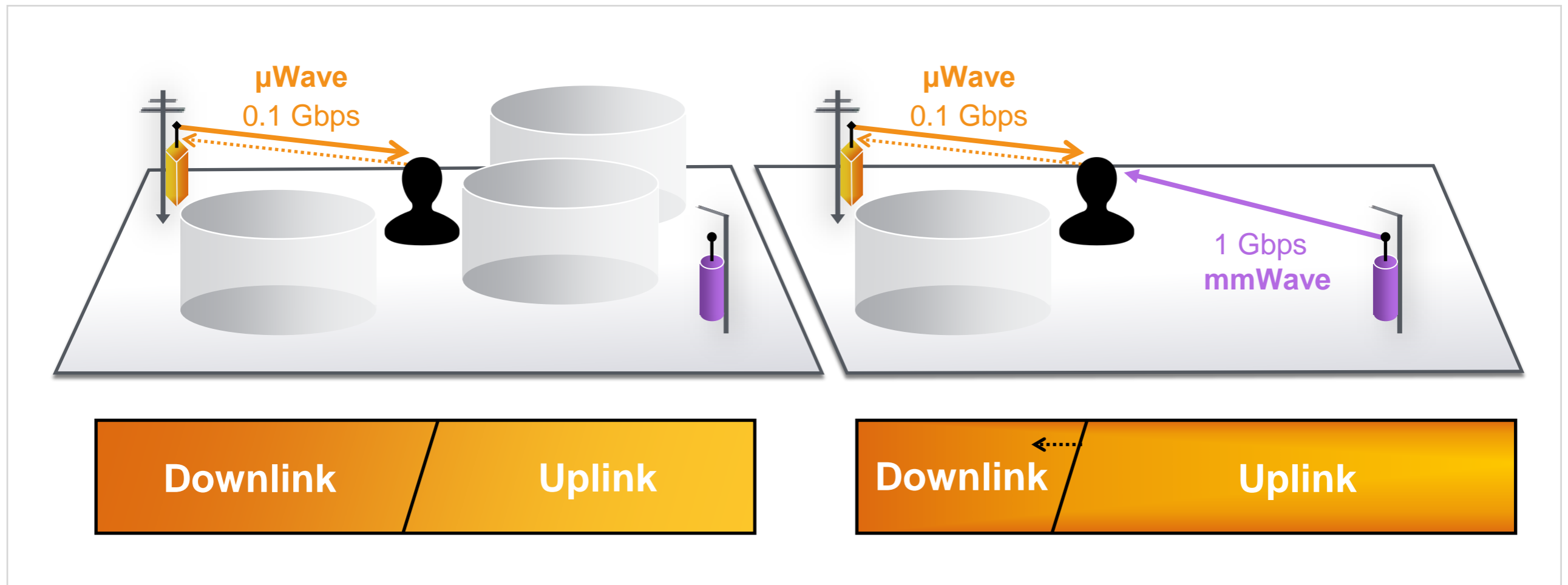
[Samsung13] W. Roh, "Performances and Feasibility of mmWave Beamforming Prototype for 5G Cellular Communications," IEEE ICC Keynote, June 2013.



# Joint Uplink/Downlink $\mu$ Wave Resource Allocation

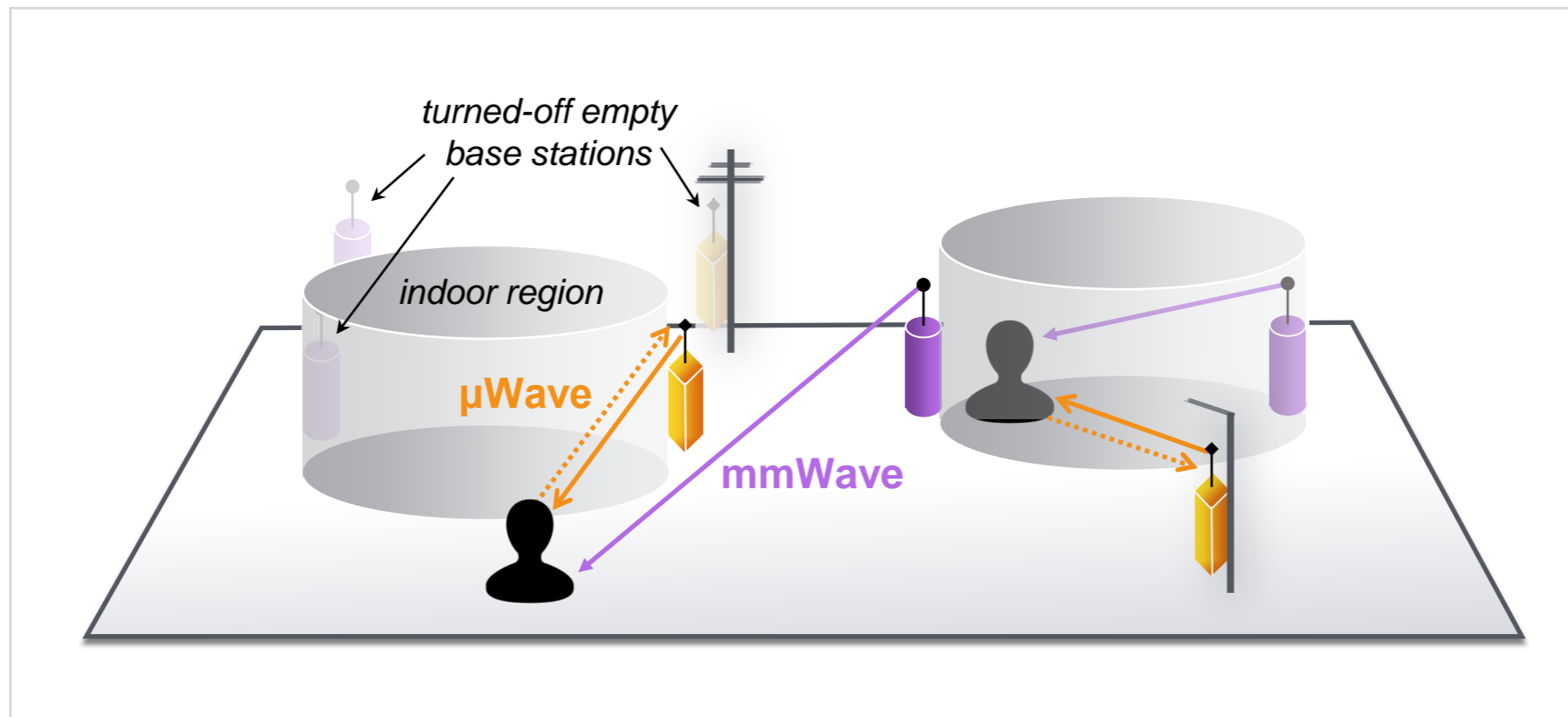
## Uplink QoS Guaranteeing $\mu$ Wave Uplink/Downlink Resource Allocation

When (downlink) mmWave is highly available,  $\mu$ Wave resource should be more allocated to uplink in order to balance the uplink/downlink rates



# Network Model

- mmWave BS locations ~ homogeneous PPP with density  $\lambda_m$
- $\mu$ Wave BS locations ~ homogeneous PPP with density  $\lambda_\mu$
- User locations ~ homogeneous PPP with density  $\lambda_u$
- Downlink only mmWave
- Dormant mode operation for empty BSs
- Maximum SNR association
- Heterogeneous carrier aggregation: receiving from both  $\mu$ Wave and mmWave if available



# Channel Model

- Boolean indoor/outdoor model with indoor grain density  $\lambda_g$  and avg. area  $S$
- $\mu$ Wave penetrable / mmWave impenetrable walls
- **mmWave:**
  - Path loss exponents: 2 for indoor /  $\alpha_m > 2$  for outdoor
  - No fading
  - Directional beam with main lobe width  $\Theta$
  - Gaussian angle-of-arrival estimation error [Rappaport13]
    - (approx.) directivity gain  $\sim \exp(1)$
- **$\mu$ Wave:**
  - Path loss exponent:  $\alpha_\mu$  for both indoor and outdoor
  - Rayleigh fading
- Interference-limited regime

# Uplink/Downlink SEs

## **μWave SE**

- Uplink/downlink reciprocity holds in ultra-dense networks
- Both Uplink and downlink SE are represented as:

$$\gamma_{\mu} > \log \left( 1 + \left[ \frac{\lambda_{\mu}}{\rho_{\mu} \lambda_u} \right]^{\alpha_{\mu}/2} \right)$$

$$\text{where } \rho_{\mu} := \int_0^{\infty} 1/(1 + u^{\alpha_{\mu}/2}) du$$

## **mmWave Downlink SE**

$$\gamma_m > \log \left( 1 + \frac{\pi \lambda_m^{(\frac{\alpha_m}{2}-1)} e^{-\lambda_g S} + 1}{\sigma^2} \left[ \frac{2\sigma^2}{\theta} \left( \frac{e^{\lambda_g S}}{\rho_m \lambda_u} \right)^{\frac{\alpha_m}{2}} \right] e^{-\lambda_g S} \right)$$

$$\text{where } \rho_m := \int_0^{\infty} 1/(1 + u^{\alpha_m/2}) du$$

# Downlink Rate Maximization While Guaranteeing Minimum Uplink Rate

## Uplink/Downlink Resource Allocation

- Average rate maximizing  $\mu$ Wave allocation
- guaranteeing the minimum uplink rate ratio  $T$

## Maximum Downlink Average Rate

$$\begin{aligned} & \text{P1. } \max_{W_\mu} R_d \\ & \text{subject to} \\ & R_u/R_d \geq T \\ & W_{\mu.d} + W_{\mu.u} = W. \end{aligned}$$



downlink mmWave SE

$$\begin{aligned} W_{\mu.u}^* &= \frac{T}{1+T} \left( W + \frac{W_m \gamma_m}{\gamma_\mu} \right) \\ W_{\mu.d}^* &= \frac{1}{1+T} \left( W - \frac{TW_m \gamma_m}{\gamma_\mu} \right) \end{aligned}$$

$$R_d^* = \frac{1}{1+T} \log \left( 1 + c_d \lambda_m^{W_m} (1 - \sqrt{\frac{S}{\lambda_m}}) \left[ \left( \frac{\alpha_m}{2} \right) e^{-\lambda_g S} + 1 \right] \lambda_\mu^{\frac{W \alpha_\mu}{2}} \right)$$

where

$$c_d = \left[ \frac{\pi}{\sigma^2} \left\{ \frac{2\sigma^2}{\theta} (\rho_m e^{-\lambda_g S} \lambda_u)^{-\frac{\alpha_m}{2}} \right\} e^{-\lambda_g S} \right]^{W_m} (1 - \sqrt{\frac{S}{\lambda_m}}) \cdot (\rho_\mu \lambda_u)^{-\frac{\alpha_\mu W}{2}}$$

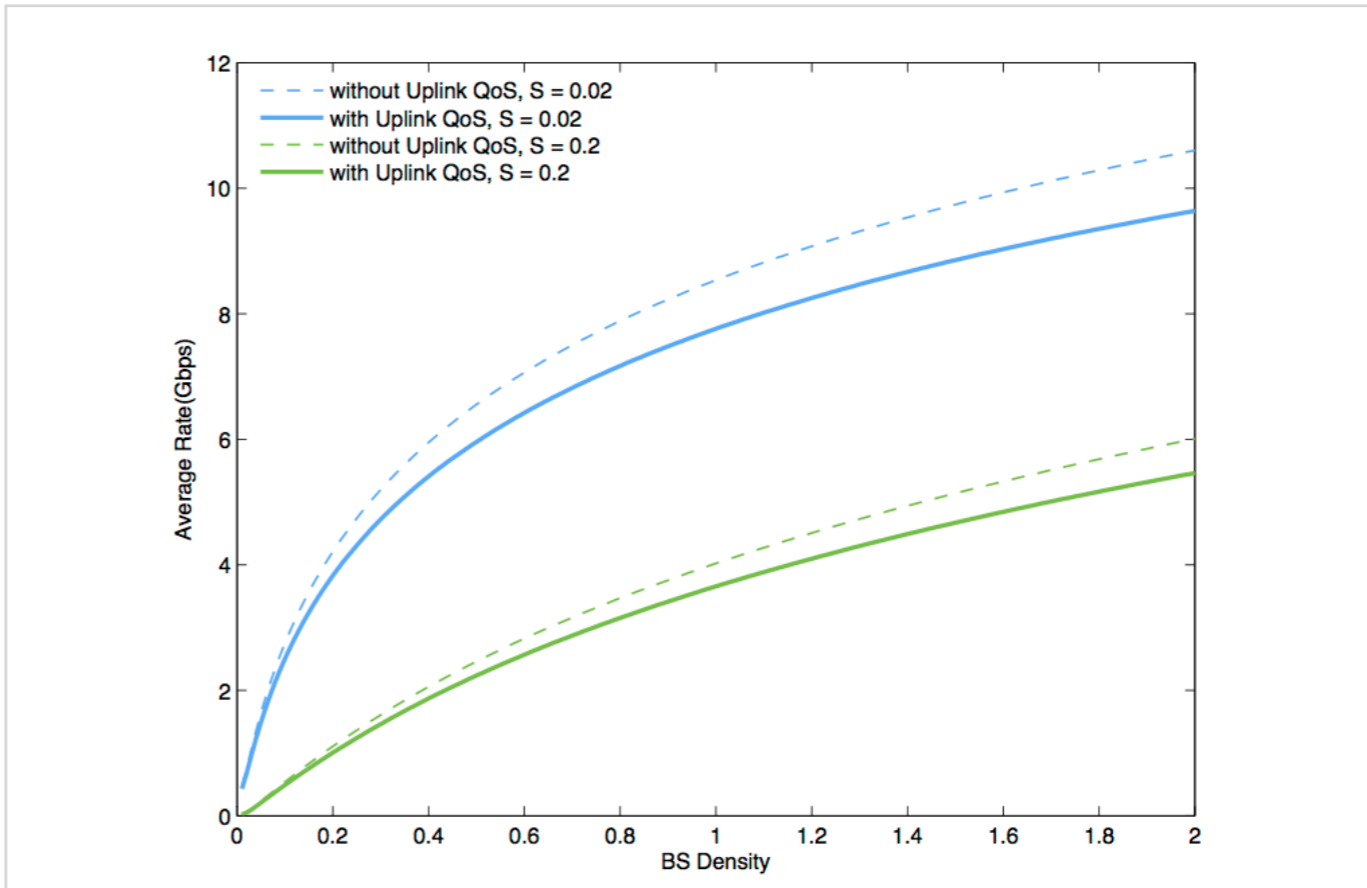


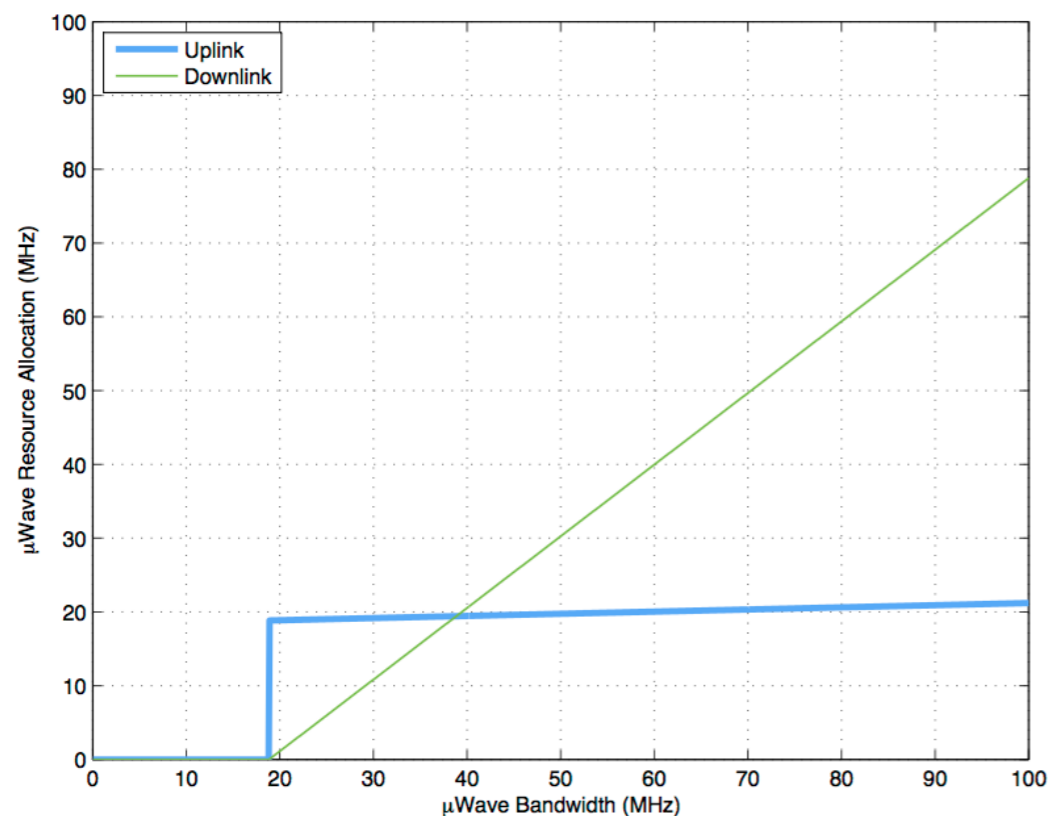
Fig. 6. Maximized downlink average rate with and without the uplink QoS  $T = 0.1$  under  $\mu$ Wave bandwidth 20 MHz and mmWave bandwidth 500 MHz ( $\lambda_u = 0.02$ ,  $\alpha_\mu = 4.58$ ,  $\alpha_m = 5.76$ ,  $\lambda_g = 0.1$ ,  $\theta = 10^\circ$ ,  $\sigma^2 = 1$ ).

# Downlink Rate Maximization While Guaranteeing Minimum Uplink Rate

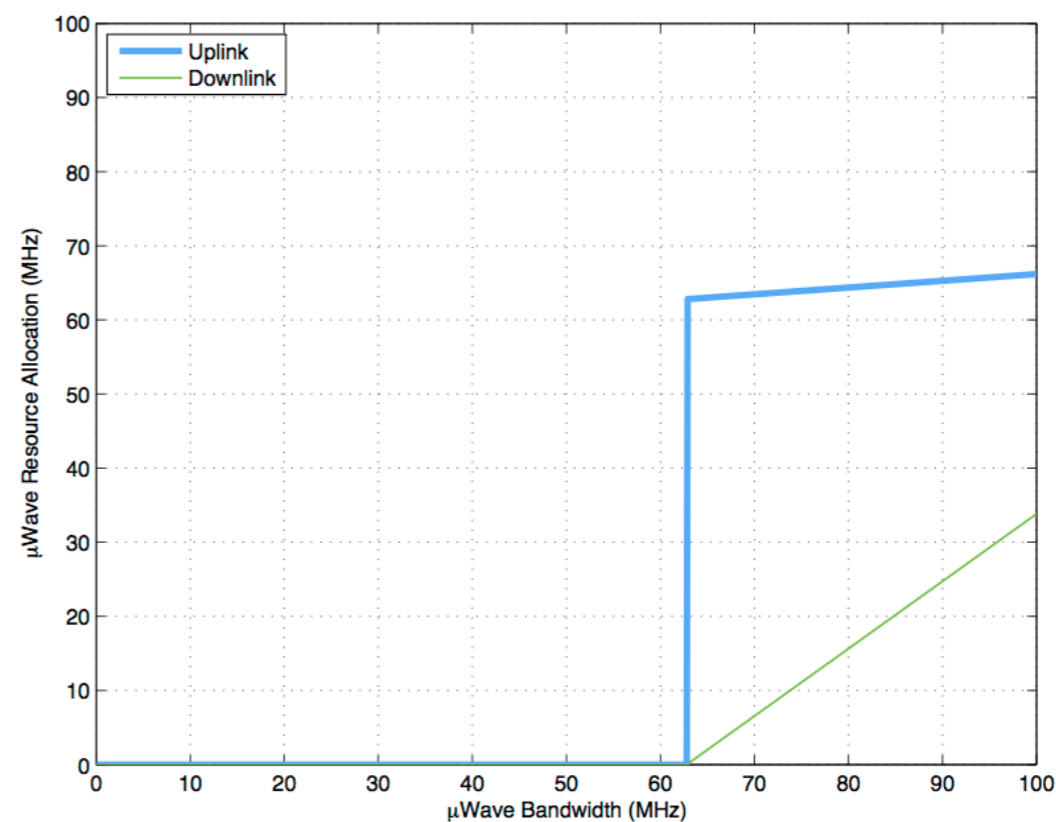
## Uplink/Downlink Resource Allocation

Result 1. (Rate Optimal  $\mu$ Wave Allocation with QoS) In a mmWave overlaid cellular network in 5G,  $\mu$ Wave uplink/downlink allocation should be:

1) mostly dedicated to the uplink; or 2) it resort to procuring additional  $\mu$ Wave spectrum



(a) Small uplink QoS requirement ( $T = 0.03$ )



(b) Large uplink QoS requirement ( $T = 0.1$ )

Fig. 5. Uplink and downlink  $\mu$ Wave resource allocations with mmWave bandwidth 500 MHz ( $\lambda_u = 0.02$ ,  $\alpha_\mu = 4.58$ ,  $\alpha_m = 5.76$ ,  $\lambda_g = 0.1$ ,  $\theta = 10^\circ$ ,  $\sigma^2 = 1$ ).

# Downlink Rate Maximization While Guaranteeing Minimum Uplink Rate

## Minimum Required $\mu$ Wave BS density for Guaranteeing Uplink Rate QoS

Result 2. (Required  $\mu$ Wave BS)  $\mu$ Wave BS densification cannot be a sole remedy for the minimum uplink QoS problem, but should be in conjunction with procuring more  $\mu$ Wave resources

$$O(\lambda_m) = \lambda_\mu \frac{\alpha_\mu W}{TW_m [(\alpha_m - 2)e^{-\lambda_g S} + 2]}$$

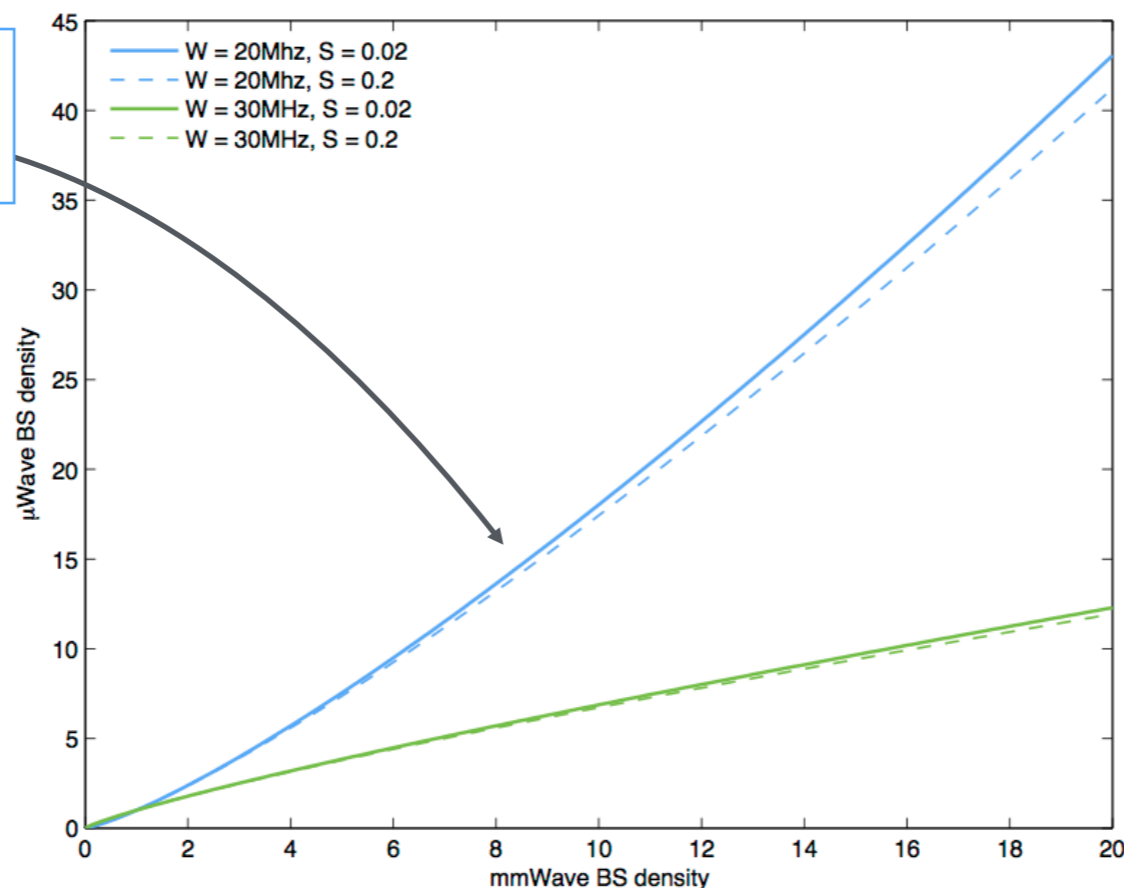


Fig. 7. Minimum required  $\mu$ Wave BS density as mmWave BS density increases for  $\mu$ Wave bandwidths 20 MHz (blue) and 30 MHz (green) under mmWave bandwidth 500 MHz ( $T = 0.04$ ,  $\lambda_u = 0.02$ ,  $\alpha_\mu = 4.58$ ,  $\alpha_m = 5.76$ ,  $\lambda_g = 0.1$ ,  $\theta = 10^\circ$ ,  $\sigma^2 = 1$ ).